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# Verification and Certification

## Using Rewriting Logic

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# Outline

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## Verification and Certification in Rewriting Logic

1. **Web Verdi-M**: a rule-based Web verification system
2. **Maude-NPA**: a crypto protocol analyzer
3. **Automated Certification** of Java Source Code in Maude



# Why rewriting logic (Maude)?

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1. **Models** and **formal specification** are easily written in Maude (Simplicity, Expressiveness, and Performance)
2. Maude provides **rewriting modulo associativity**, **commutativity** and **identity**
3. Differentiation between **concurrent** and **deterministic fragments** of a model, differentiation between **non-terminating** and **terminating fragments** of a model
4. It provides **order-sorted** specifications
5. It provides an infrastructure for formal analysis and verification (including a **search** command, a **LTL model checker**, a **theorem prover**, etc.)
6. **Reflection** (meta-modeling, symbolic execution, etc.)
7. **Models of computation** ( $\lambda$ -calculi,  $\pi$ -calculus, petri nets, CCS), **Programming languages** (Java, Haskell, Prolog), **Distributed algorithms and systems** (real-time, probabilistic), **Biological systems** in Maude



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# Web Verdi-M

(A rule-based Web verification system)

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# Web Verdi-M : Goals

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- Web Service and web client for verification of web sites w.r.t. an intended behavior.
- Optimization and repairing support.



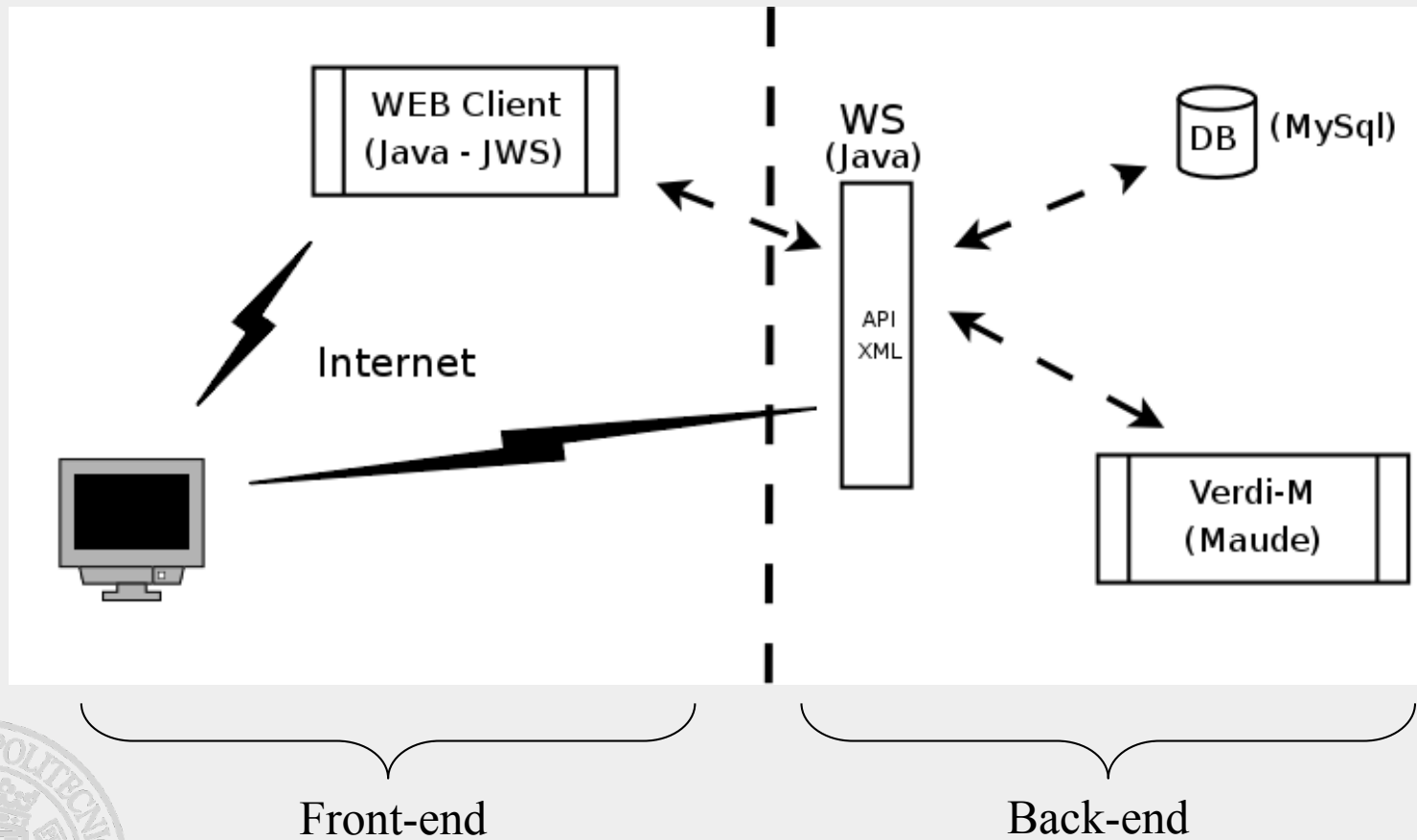
# Intended Behavior

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- We have a specification language to verify if a web site is correct w.r.t. its specification.
- This specification contains **rules**:
  - Correctness rules (for detecting incorrect web pages). These rules have the following form:
    - $\text{member}(\text{name}( X ) , \text{surname}( Z ) ) \rightarrow \text{error} : X == Z$
  - Completeness rules (for detecting information incomplete and/or missing web pages). These rules have the following form:
    - $\text{hpage}(\text{status}( \text{Professor} ) ) \rightarrow \# \text{hpage}(\# \text{status}( \# \text{Professor} ) , \text{teaching}( ) ) < A >$



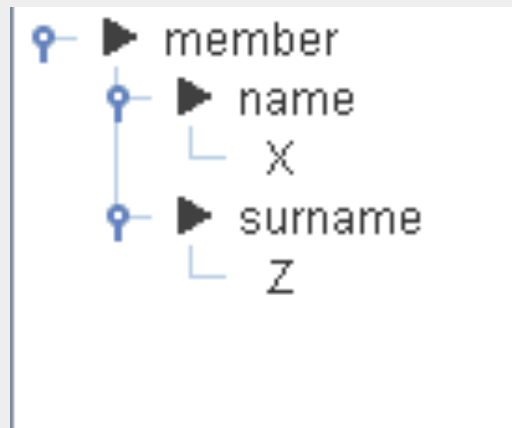
# Web Verdi-M: Architecture



# Graphical interface

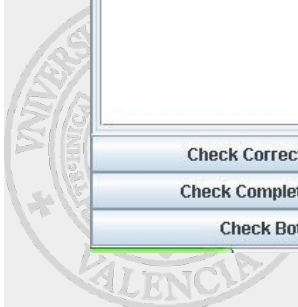
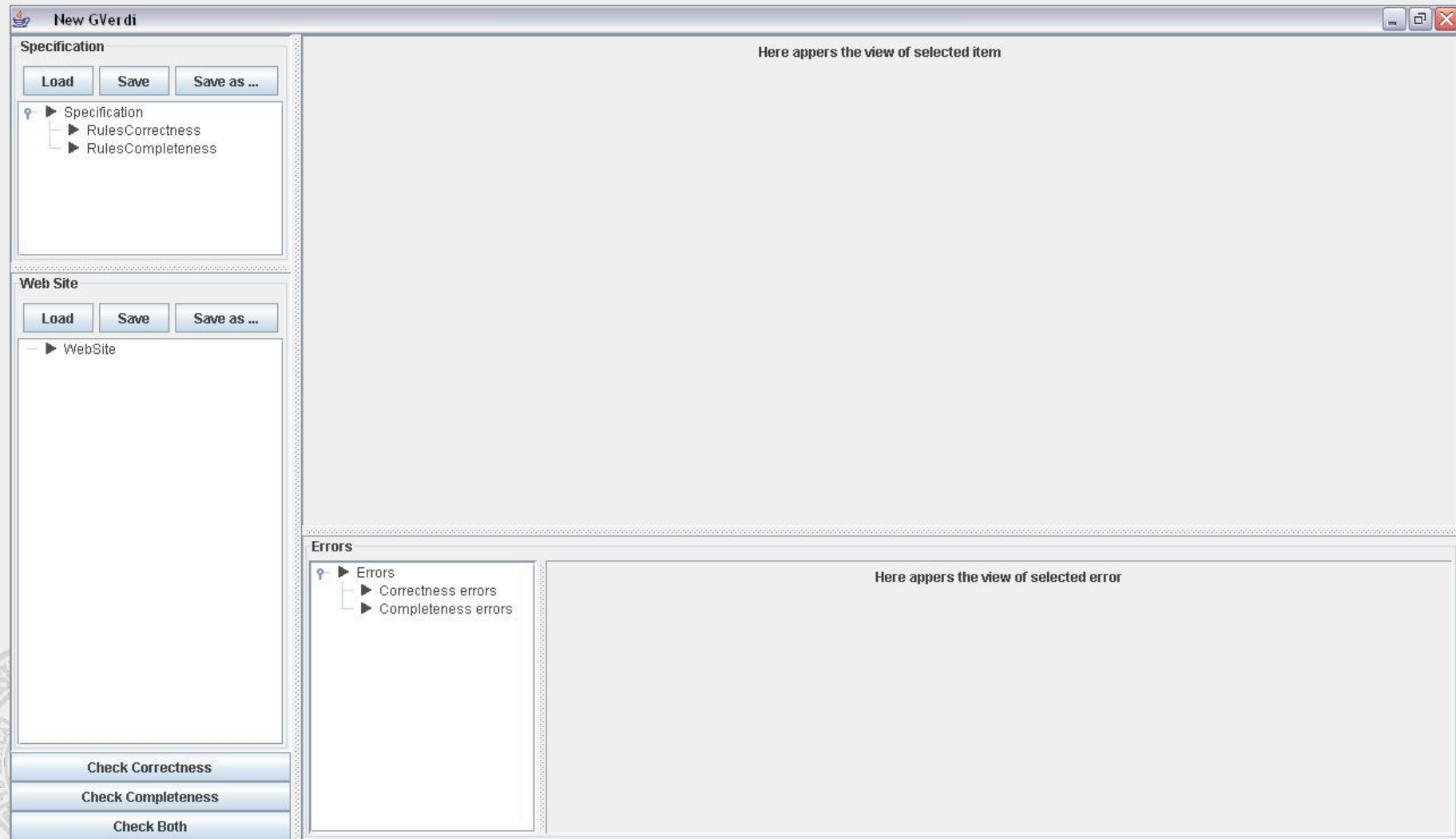
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- The graphical interface is based on tree directories.
- Example:
  - `member(name(X),surname(Z))`





# Main Window



# Web Site Panel

Web Site

Load Save Save as ...

- WebSite
  - p1 - pageAnnaGialli.html
  - p4 - pageMembers.html
  - p2 - pageFrancaBianchi.html
  - p5 - pagePubs.html
  - p3 - pageMarioRossi.html

Web Site

Load Save Save as ...

- WebSite
  - Add web page
  - p1 - pageAnnaGialli.html
  - p4 - pageMembers.html
  - p2 - pageFrancaBianchi.html
  - p5 - pagePubs.html
  - p3 - pageMarioRossi.html

Web Site

Load Save Save as ...

- WebSite
  - p1 - pageAnnaGialli.html
  - p4 - pageMembers.html
  - p2 - pageFrancaBianchi.html
  - p5 - pagePubs.html
  - p3 - pageMarioRossi.html

Remove web page



# Check Rules - Options

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Check Correctness

- Check via the web service, the correctness rules loaded.

Check Completeness

- Check via the web service, the completeness rules loaded.

Check Both

- Check via the web service, the correctness and completeness rules loaded.



# Error Views – Correctness(1)

View the correctness error - Error 1

Graphical View XML View

Error 1

- pid
- w
- left
- sigma
- condition

member

- name
  - X
- surname
  - Z



# Error Views – Correctness(2)

View the correctness error - Error 1

Graphical View XML View

```
<errorCorrectness>
  <pid> p4 </pid>
  <w> 1.4 </w>
  <l>
    <member>
      <name> X </name>
      <surname> Z </surname>
    </member>
  </l>
  <sigma>
    <sust>
      <var> X </var>
      <value>
        'Verdi'
      </value>
    </sust>
    <sust>
      <var> Z </var>
      <value>
        'Verdi'
      </value>
    </sust>
  </sigma>
</errorCorrectness>
```



# Error Views – Completeness(1)

View the completeness error - Error 1

Graphical View XML View

Left: Right:

Quantifier:

- Universal
- Existential

```
graph TD
    subgraph Graphical_View [Graphical View]
        Error1[Error 1]
        Error1 --- rule
        Error1 --- pages
        Error1 --- sigma
        Error1 --- type
    end

    subgraph XML_View [XML View]
        subgraph Left
            hpage_L[hpage]
            hpage_L --- status_L[status]
            status_L --- Prof_L['Professor']
        end
        subgraph Right
            hpage_R[hpage]
            hpage_R --- status_R[status]
            status_R --- Hash_R[# 'Professor']
            hpage_R --- teaching_R[teaching]
        end
    end

    subgraph Quantifier [Quantifier]
        Universal((Universal))
        Existential((Existential))
    end
```



# Error Views – Completeness(2)

View the completeness error - Error 1

Graphical View XML View

```
<hpage>
  <status> 'Professor' </status>
</hpage>
</left>
<right>
  <hpage Mark="true">
    <status Mark="true"> #'Professor' </status>
    <teaching>
    </teaching>
  </hpage>
</right>
<quantifier> A </quantifier>
</r>
<pages>
  <pid> p3 </pid>
  <pid> p1 </pid>
</pages>
<sigma>
</sigma>
<type> A </type>
</errorCompleteness>
```



# Extensions and Optimizations

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- Abstract Verification (via Source-to Source Compression Transformation)
- Ontology reasoning





# Maude-NPA: crypto protocol analyzer

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Catherine Meadows (Naval Research Laboratory, USA)

José Meseguer (University of Illinois at Urbana-Champaign, USA)

Sonia Santiago (Universidad Politécnica de Valencia, Spain)

Carolyn Talcott (SRI International, USA)



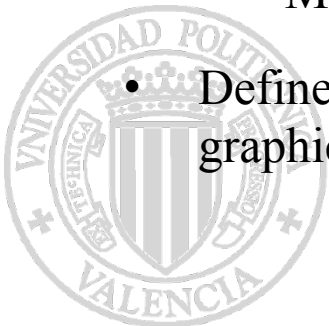
## General Maude-NPA Goal

- Crypto protocol analysis with the [standard free algebra model](#) (“Dolev-Yao”) well understood
- [Extend](#) standard free algebra model of crypto protocol analysis to deal with [algebraic properties](#):
  1. Encryption-decryption
  2. Diffie Hellman
  3. Exclusive-or, etc.
- Provide tool than can be used to reason about protocols with these [algebraic properties](#) in the [unbounded](#) session model
- Provide [graphical interface](#) for analysis, interaction and validation of crypto protocols



# Overview of Maude-NPA

- Use **rewriting logic** as general theoretical framework
  - **rewrite rules** are obtained from strands
  - algebraic identities as **equational properties** and axioms
- Use narrowing modulo equational theories in two ways
  - as a **symbolic reachability analysis method**
  - as an **extensible equational unification method**
- Combine with state reduction techniques of NRL Protocol Analyzer (grammars, optimizations, etc.)
- Implement in **Maude** programming environment
  - Rewriting logic gives us **theoretical framework** and understanding
  - Maude implementation gives us **tool support**
- Define graphical interface within Maude and its associated frameworks for graphical interaction (IOP, IMaude and JLamba)



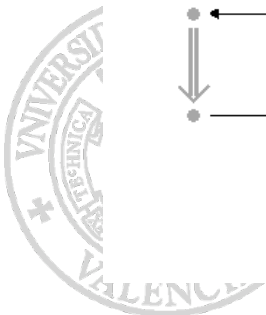
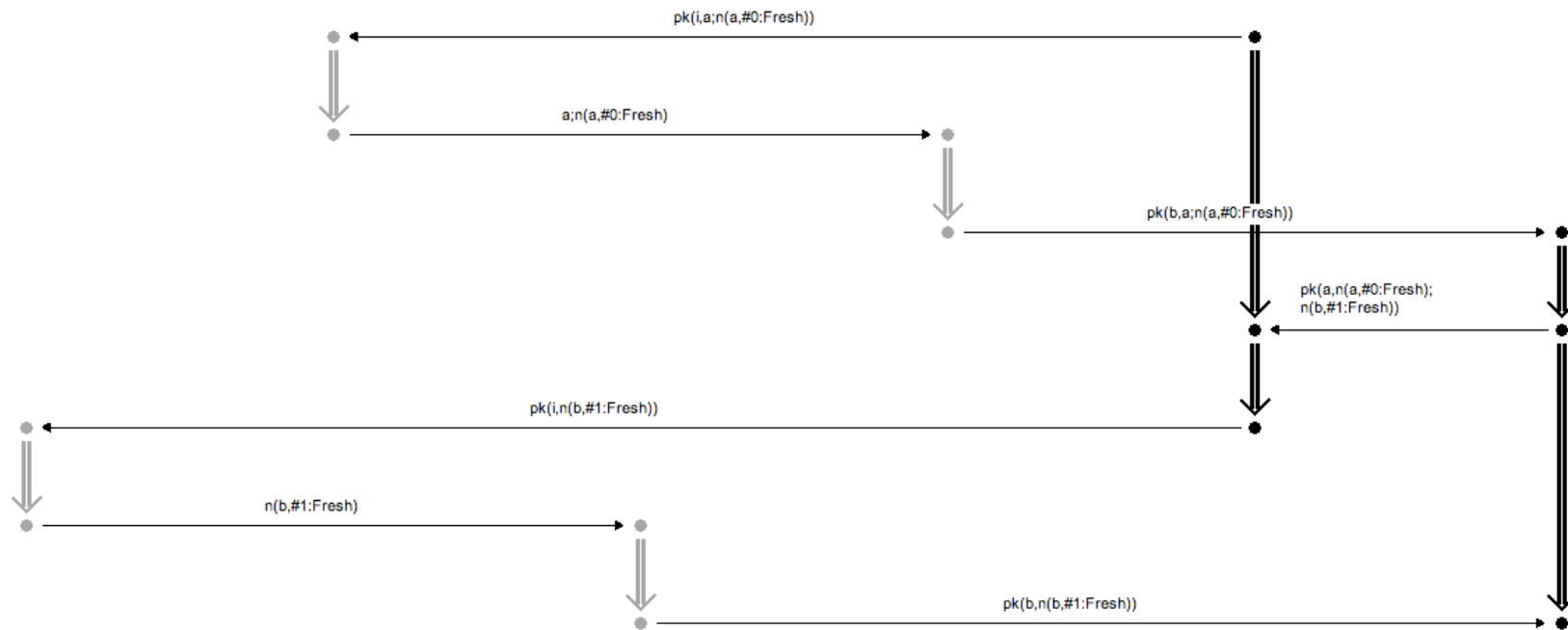
# Maude-NPA

- A tool to **find** or **prove the absence** of attacks using **backwards search**
- Analyzes **infinite state systems**
  - **Active intruder**
  - **No abstraction or approximation** of nonces
  - **Unbounded** number of sessions
- **Intruder** and **honest** protocol transitions represented using variant of strand space model
- Algebraic identities such as **exponentiation** and **Encryption/Decryption** cancellation identities included
- Uses modified strand space model
- Each local execution and each intruder action represented by a strand, plus a marker denoting the current state
  - Searches backwards through strands from final state.
  - Set of rewrite rules governs how search is conducted
  - Sensitive to past and future
- Grammars and other optimizations used **to prevent infinite loops** and avoid some transitions



# How protocols are specified in Maude-NPA

- Represent protocols and intruder actions using strands
  - Strands may contain variables, except for terms of type *Fresh*, which are always constant (used by *nonces*)
  - Strand annotated with fresh terms generated by principal executing strands
  - $:: r :: [\text{pke}(B, n(A, r); A)^+, \text{pke}(A, n(A, r); NB)^-, \text{pke}(B, NB)^+]$



# Diffie-Hellman Protocol

- Protocol

$A \rightarrow B: A ; B ; \text{exp}(g, N\_A)$

$B \rightarrow A: A ; B ; \text{exp}(g, N\_A)$

$A \rightarrow B: \text{enc}(\text{exp}(\text{exp}(g, N\_B) , N\_A), \text{secret}(A,B))$

- Equational Theory Algebraic properties

$B = \{ (X * Y) * Z = X * (Y * Z), (X * Y) = Y * X \}$

$\Delta = \{ \text{exp}(\text{exp}(W, Y), Z) = \text{exp}(W, Y * Z) \}$

Can B in a session apparently in A without A engaging in the corresponding session?



# Main Window

The screenshot displays the 'Attack a0 (tree0)' window. At the top, there is a 'File Window' menu and a toolbar with icons for navigation and search. The main area contains a hierarchical tree diagram with nodes labeled with IP addresses in angle brackets. The node '<1.5.2.7.2.4.3.1>' is highlighted in green. To the right, a 'Find Node' panel lists the nodes in the tree, with '<1.5.2.7.2.4.3.1>' selected. Below the list are 'Find' and 'Click' buttons. A vertical sidebar on the right contains buttons for 'Find', 'Context Menu', 'Info', and 'Window Manager'.

```
graph TD;
  Root["<>"] --> L1["<1>"];
  L1 --> L15["<1.5>"];
  L1 --> L12["<1.2>"];
  L1 --> L17["<1.7>"];
  L15 --> L154["<1.5.4>"];
  L15 --> L152["<1.5.2>"];
  L12 --> L1213["<1.2.13>"];
  L17 --> L174["<1.7.4>"];
  L154 --> L1543["<1.5.4.3>"];
  L152 --> L1527["<1.5.2.7>"];
  L1527 --> L15272["<1.5.2.7.2>"];
  L1527 --> L15278["<1.5.2.7.8>"];
  L15272 --> L152724["<1.5.2.7.2.4>"];
  L15278 --> L152783["<1.5.2.7.8.3>"];
  L152724 --> L1527243["<1.5.2.7.2.4.3>"];
  L152724 --> L1527242["<1.5.2.7.2.4.2>"];
  L1527243 --> L15272431["<1.5.2.7.2.4.3.1>"];
  L1527242 --> L15272424["<1.5.2.7.2.4.2.4>"];
  L1527242 --> L15272422["<1.5.2.7.2.4.2.2>"];
  L15272424 --> L152724243["<1.5.2.7.2.4.2.4.3>"];
  L15272422 --> L152724227["<1.5.2.7.2.4.2.2.7>"];
  style L15272431 fill:#00FF00
```



# State info

Textual information of node <(1[2]).6.4>

Window

Show strands  Show intruder knowledge  Show sequence of messages  Show additional information

Select the information you want to view. Then, you can also deselect the information you don't want to see.

Current Strands

```
-----
:: nil :: [ nil | - ( a ) , - ( #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) , + ( a ; #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) , nil ] &
:: #0:Fresh :: [ nil , - ( a ; b ; exp ( #1:Gen , n ( a , #2:Fresh ) ) ) , + ( a ; b ; exp ( g , n ( b , #0:Fresh ) ) ) | - ( e ( exp ( #1:Gen , n ( a , #2:Fresh ) <+> n ( b , #0:Fresh ) ) , sec ( a , #3:Fresh ) ) ) , nil ] &
:: #2:Fresh , #3:Fresh :: [ nil , + ( a ; #4:Name ; exp ( g , n ( a , #2:Fresh ) ) ) | - ( a ; #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) , + ( e ( exp ( #1:Gen , n ( a , #2:Fresh ) <+> n ( b , #0:Fresh ) ) , sec ( a , #3:Fresh ) ) ) , nil ]
```

Intruder knowledge

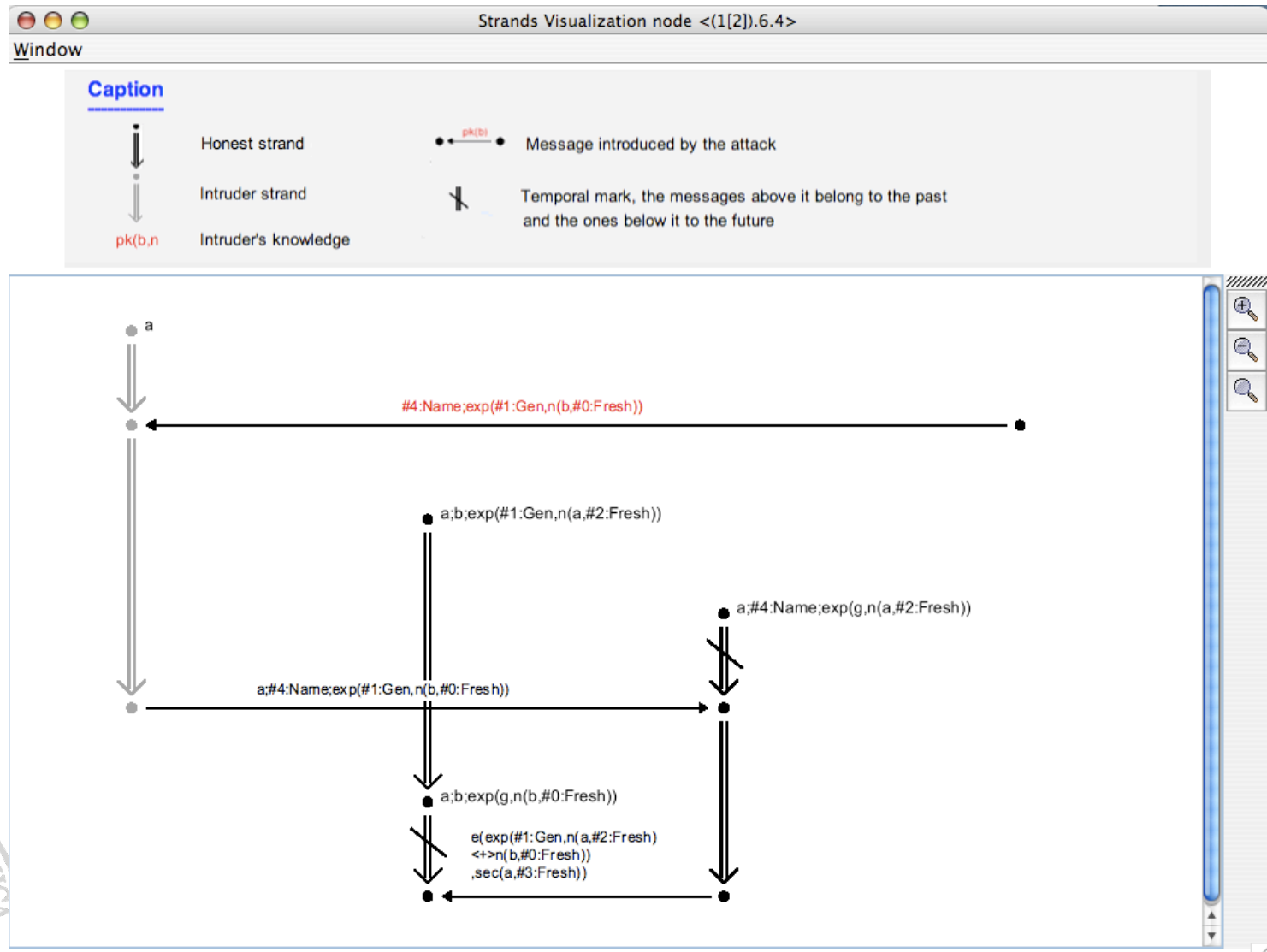
```
-----
e ( exp ( #1:Gen , n ( a , #2:Fresh ) <+> n ( b , #0:Fresh ) ) , sec ( a , #3:Fresh ) ) !inl ,
( a ; #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) !inl ,
( #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) inl ,
inst ( #1:Gen )
```

Sequence of messages

```
-----
- ( a ) ,
- ( #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) ,
+ ( a ; #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) ,
- ( a ; #4:Name ; exp ( #1:Gen , n ( b , #0:Fresh ) ) ) ,
+ ( e ( exp ( #1:Gen , n ( a , #2:Fresh ) <+> n ( b , #0:Fresh ) ) , sec ( a , #3:Fresh ) ) ) ,
- ( e ( exp ( #1:Gen , n ( a , #2:Fresh ) <+> n ( b , #0:Fresh ) ) , sec ( a , #3:Fresh ) ) )
```



# Graphical view of Strands for each state





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# A Tool for Automated Certification of Java Source Code in Maude

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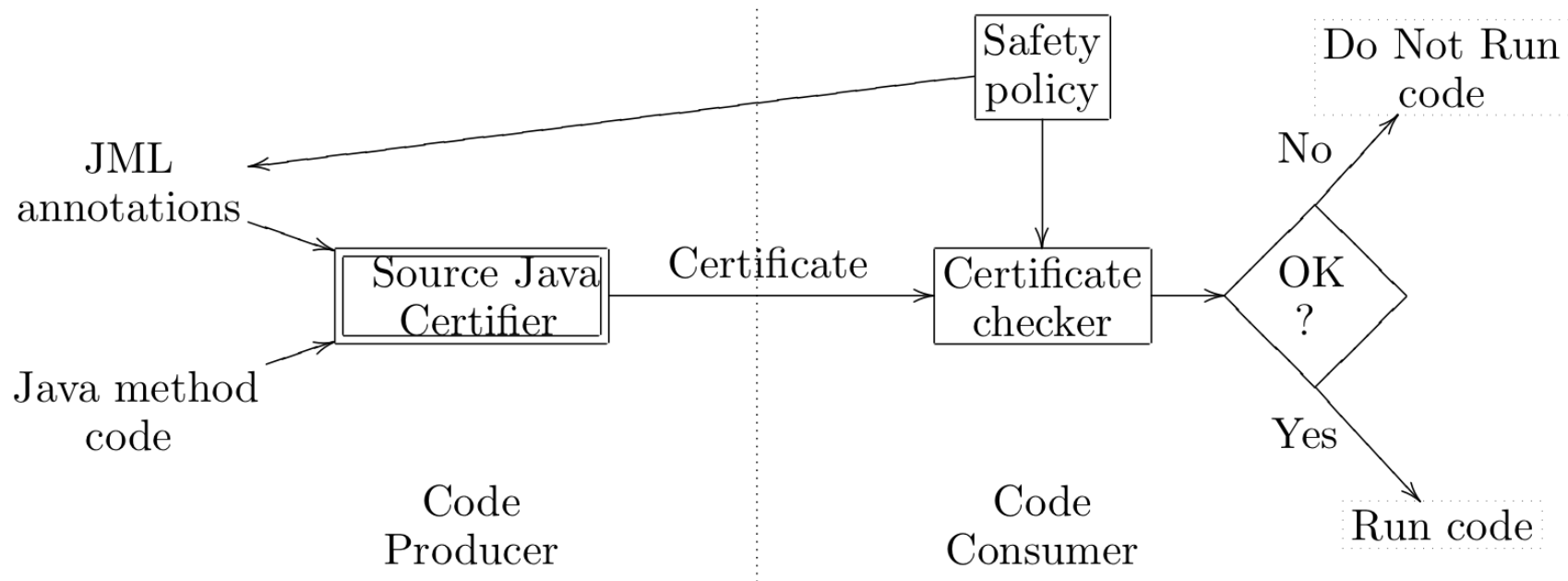
Pedro Ojeda (Universidad Politécnica de Valencia, Spain)

Daniel Romero (Universidad Nacional de Río Cuarto, Argentina)



# Proof-Carrying Code Scheme in Maude

- Proof-Carrying Code based on rewriting logic (Maude)



# Abstract Reachability Analysis

---

- **Producer (certificate generator):**
  - Uses abstract operational semantics of Java written in Maude
  - Chooses an abstract domain suitable for the safety properties to be certified
  - Initial and final abstract reachability states are inferred from safety properties
  - Applies abstract reachability analysis
- **Safety Certificate:**
  - Consists of abstract rewriting sequences (performed by Maude)
  - Generated from search command in Maude
  - Demonstrate unreachability of unsafe states, i.e. those undesired states which are inferred from safety property



# Safety Policies specified in JML

---

- Arithmetic:

```
static int summation(int n)    {
/*@ requires AbsValue(n) == 0A || AbsValue(n) == 3A;
   @ ensures AbsValue(\result) == evenA ; @*/
int sum = 0 ;
int i = 0;
/*@ assert AbsDomain(sum) == EvenOdd &&
          AbsDomain(i) == (Mod4, (<=, n)); @*/
while (i <= n) {
    sum += i;
    i ++;
}
return sum;
}
```



# Safety Policies specified in JML

---

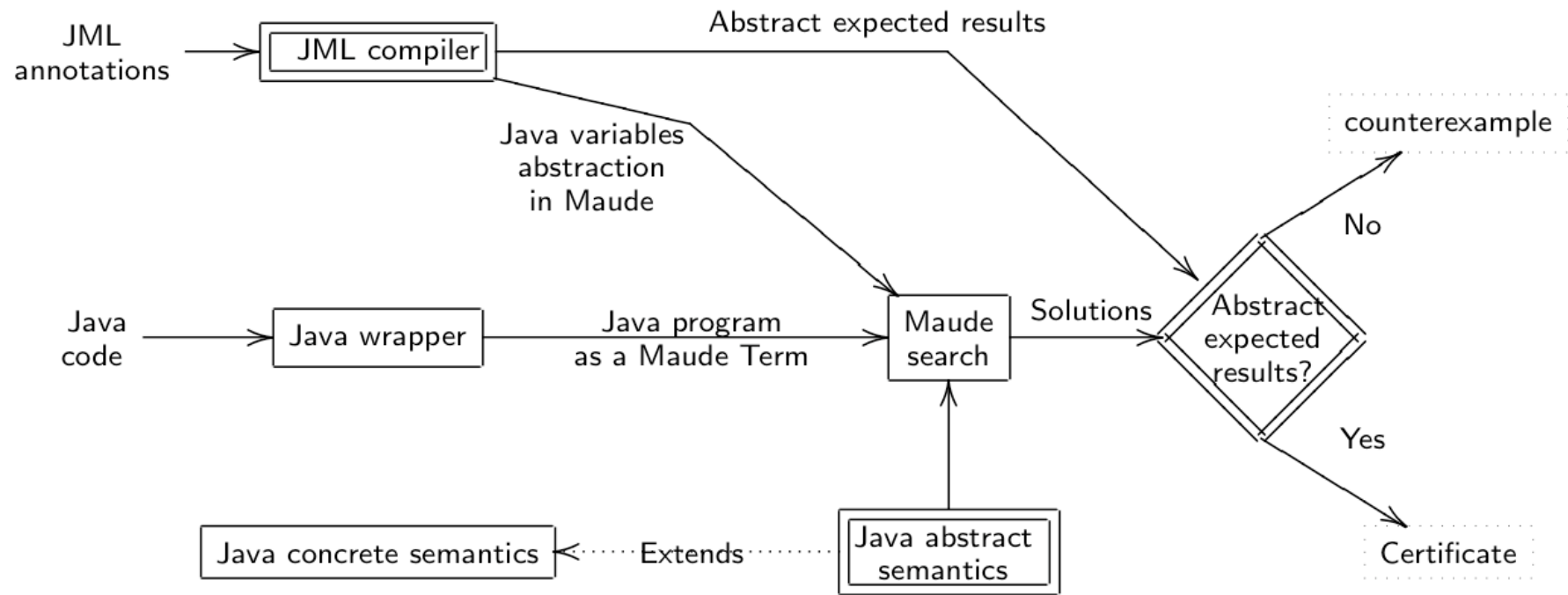
- Non-interference:

```
public int m1(int high, int low) {
  /*@ requires AbsValue(high) == highA && AbsValue(low) == lowA;
    @ ensures AbsValue(\result) == lowA; @*/
  low = high;
  low = 2;
  return low;
}
```

```
public int m2(int high, int low) {
  /*@ requires AbsValue(high) == highA && AbsValue(low) == lowA;
    @ ensures AbsValue(\result) == lowA; @*/
  while (true) {
    high --;
    low ++;
    if (low > high)
      break;
  }
  return low;
}
```



# PCC Overview



# Main Windows

The image shows two windows from the 'Automatic Certification of Java Source Code in Rewriting Logic' application. The left window is the main interface, and the right window is a Mozilla Firefox browser displaying the application's output.

**Main Interface (Left Window):**

- Title:** Automatic Certification of Java Source Code in Rewriting Logic - Mozilla Firefox
- Menu:** Archivo, Editor, Ver, Historial, Marcadores, Herramientas, Ayuda
- Section:** Automatic Certification of Java Source Code in Rewriting Logic
- Left Panel:**
  - Selected program: ExampleNoninterference2.java
  - Load from disk: [ ] [Examinar...] [load]
  - Java Code (from Example: ExampleNoninterference2.java):

```
// This example DOES COMPLY the non-interferenc
/*@ requires AbsValue(low) == lowA && AbsValue(
  @ ensures AbsValue(\result) == lowA;

public int mE1(int high, int low) {
  low = high;
  low = 2;
  return low;
}
```
  - status: syntax valid
- Right Panel:**
  - Select method: mE1
  - Select safety property: Non Interference
  - Options:
    - Verification only
    - With reduced label certificate
    - With reduced rules certificate
    - With full certificate
  - [Certify!]

**Output Window (Right Window):**

- Title:** Certificate - Mozilla Firefox
- Section:** With full certificate
- Safety property:** Non Interference
- Program:** Example: ExampleNoninterference2.java
- Method:** mE1
- JML specification:**

```
/*@ requires AbsValue(low) == lowA && AbsValue(high) == highA;
   @ ensures AbsValue(\result) == lowA;          @*/
```
- Policy:**  Satisfy
- Certificate:**

```
search in PGM-SEMANTICS-DATAFLOW-ABSTR : javaLabel((preprocess(default class t(
  'myClass) imports nil extends Object implements none (public int 'mE1((int
  d('high),(int d('low))throws(noType) {(6 @ ('low = 'high ;)) 7 @ ('low =
  1(2) ;)) 8 @ return 'low ;} (public static) void 'main(t('String[]) d(
  'arg))throws(noType) {(((((((int d('even) = i(0) ;) (int d('odd) = i(1)
  ;)) (int d('n0) = i(0) ;)) (int d('n1) = i(1) ;)) (int d('n2) = i(2) ;)) (
  int d('n3) = i(3) ;)) (int d('low) = i(0) ;)) (int d('high) = i(1) ;)) 23 @
  {'System . 'out . 'println < 'mE1 < 'low,'high > > ;}}) noType . 'main <
  new string [i(0)] > noVal)) =>! X:Output .

***** equation
eq t('String) = string .
empty substitution
t('String)
--->
string
***** equation
eq preprocess(CI) = removeImports(reformatConstri(changeType(CI))) .
CI --> default class t('myClass) imports nil extends Object implements none {
  public int 'mE1((int d('high),(int d('low))throws(noType) {(6 @ ('low =
  'high ;)) (7 @ ('low = i(2) ;)) 8 @ return 'low ;} (public static) void
  'main(string[] d('arg))throws(noType) {(int d('even) = i(0) ;) (int d('odd)
```

